

Discussion of

**The Lead-Lag Relationship between VIX Futures and SPX Futures**  
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# Lead-lag relationship

One market often follows the movements of another **with a time delay**

- e.g., SPX vs. SPX futures/options; SPX vs. SPX-tracking ETFs

Why do we observe lead-lag patterns?

- (1) Information channel: some markets might reflect information faster
- (2) Hedging channel: market makers' hedging activities create a cross-market relation

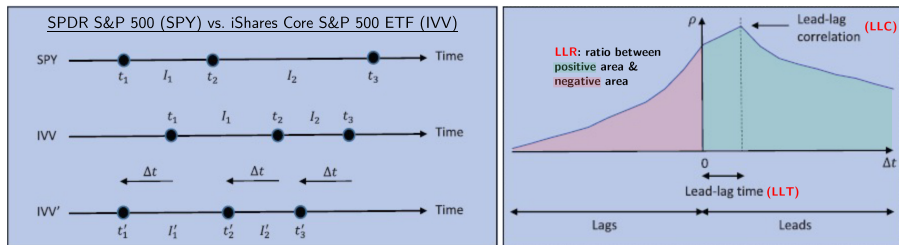
This paper focuses on the **latter channel** between **VIX futures** vs. **SPX futures**

- Very relevant topic with policy implications
- Pitfalls of dealers' hedging/rebalancing
  - ▶ “Gamma traps” (DeSimone, 2020); “Vol-mageddon” (Augustin, Cheng & Van den Bergen, 2021)

## Ultra-high-frequency data (tick data in milliseconds)

- Main challenge: **non-synchronously observed** data points
- Solution: **correlation curve** (Hayashi & Yoshida, 2005; Hoffmann, Rosenbaum & Yoshida, 2013)

## An illustrative example (Dao, McGroarty & Urquhart, 2018)

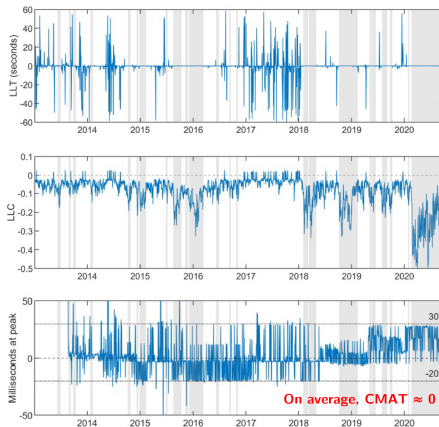
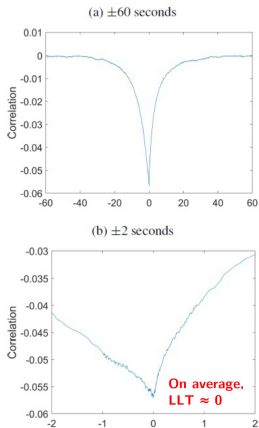


We can measure **co-occurrences of market activities** instead of price comovements

- CMAT and PCMA (Dobrev & Schaumburg, 2017)

## Comment 1: Do we observe a clear lead-lag pattern?

On average,  $LLT \simeq 0$  and  $CMAT \simeq 0$



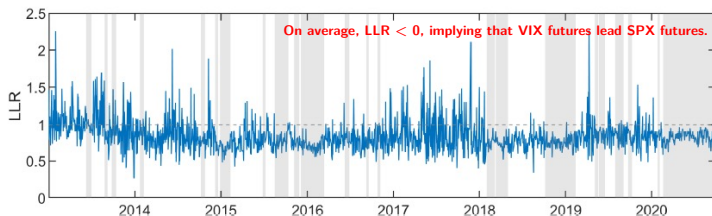
Moreover, LLC (lead-lag strength) becomes high whenever  $LLT \simeq 0$

- The correlation between the two markets is strongest when  $LLT \simeq 0$



## Comment 2: LLR vs. LLT/CMAT

Hence, the paper's empirical analysis mainly relies on LLR



- It is a bit self-serving to say that LLR is a “more robust measure of the lead-lag relation” because LLR produces more favorable results

Can we say **VIX futures lead SPX futures** because  $LLR < 0$  (when  $LLT \simeq 0$ )?

- The authors argue that other market activities “could strengthen VIX futures’ lead while pushing the LLT towards zero”
- It would be nice to elaborate on this, making the mechanism clear

## Comment 3: Cross-market activities

**The paper argues that cross-market activities mainly drive the lead-lag pattern**

- LLR is regressed on  $PCMA_t \cdot 1_{\{CMAT_t \leq 0\}}$  and  $PCMA_t \cdot 1_{\{CMAT_t > 0\}}$
- Main result: LLR is loaded on  $PCMA_t \cdot 1_{\{CMAT_t \leq 0\}}$  with a negative sign

**But, CMAT is also a lead-lag measure**

$$\begin{cases} \text{VIX futures lag} & \Rightarrow & \text{LLR} > 0 & \text{and} & PCMA_t \cdot 1_{\{CMAT_t \leq 0\}} = 0 \\ \text{VIX futures lead} & \Rightarrow & \text{LLR} \leq 0 & \text{and} & PCMA_t \cdot 1_{\{CMAT_t \leq 0\}} > 0 \end{cases}$$

- Thus, the negative sign might be a **mechanical outcome**

**Another issue: LLR is also loaded on  $PCMA_t \cdot 1_{\{CMAT_t > 0\}}$  with a negative sign**

- This is odd and inconsistent with the paper's story
- Perhaps, this is why the authors do not regress LLR on PCMA itself?

## Comment 4: Interpretation of the lead-lag relationship

### Hidden premise: VIX futures' lead comes from hedging activities

- I feel like there is a **logical gap** here
- What about the volatility feedback effect?

### **One simple thing to check**

- The authors find that uninformed VIX futures trading (e.g., **rebalancing of VIX ETPs**) does affect SPX futures' prices
- Do we observe a **stronger lead-lag relationship** on those rebalancing days?

# Conclusion

- Interesting paper!
- Understanding the relation between the two markets is important
- The paper will benefit from a consistent story that can tie things together
- I am looking forward to reading the next version!